| Topic/Skill | Definition/Tips | Example |
| :---: | :---: | :---: |
| 1. <br> Simultaneous Equations | A set of two or more equations, each involving two or more variables (letters). <br> The solutions to simultaneous equations satisfy both/all of the equations. | $\begin{gathered} 2 x+y=7 \\ 3 x-y=8 \\ x=3 \\ y=1 \end{gathered}$ |
| 2. Variable | A symbol, usually a letter, which represents a number which is usually unknown. | In the equation $x+2=5, x$ is the variable. |
| 3. Coefficient | A number used to multiply a variable. <br> It is the number that comes before/in front of a letter. | $6 z$ <br> 6 is the coefficient z is the variable |
| 4. Solving Simultaneous Equations (by Elimination) | 1. Balance the coefficients of one of the variables. <br> 2. Eliminate this variable by adding or subtracting the equations (Same Sign Subtract, Different Sign Add) <br> 3. Solve the linear equation you get using the other variable. <br> 4. Substitute the value you found back into one of the previous equations. <br> 5. Solve the equation you get. <br> 6. Check that the two values you get satisfy both of the original equations. | $\begin{gathered} 5 x+2 y=9 \\ 10 x+3 y=16 \end{gathered}$ <br> Multiply the first equation by 2 . $\begin{aligned} & 10 x+4 y=18 \\ & 10 x+3 y=16 \end{aligned}$ <br> Same Sign Subtract ( +10 x on both) $y=2$ <br> Substitute $y=2$ in to equation. $\begin{gathered} 5 x+2 \times 2=9 \\ 5 x+4=9 \\ 5 x=5 \\ x=1 \end{gathered}$ <br> Solution: $x=1, y=2$ |
| 5. Solving Simultaneous Equations (by Substitution) | 1. Rearrange one of the equations into the form $y=$... or $x=$... <br> 2. Substitute the right-hand side of the rearranged equation into the other equation. <br> 3. Expand and solve this equation. <br> 4. Substitute the value into the $y=\ldots$ or $x=$... equation. <br> 5. Check that the two values you get satisfy both of the original equations. | $\begin{gathered} y-2 x=3 \\ 3 x+4 y=1 \end{gathered}$ <br> Rearrange: $y-2 x=3 \rightarrow y=2 x+3$ <br> Substitute: $3 x+4(2 x+3)=1$ <br> Solve: $3 x+8 x+12=1$ $\begin{gathered} 11 x=-11 \\ x=-1 \end{gathered}$ <br> Substitute: $y=2 \times-1+3$ $y=1$ <br> Solution: $x=-1, y=1$ |


| 6. Solving Simultaneous Equations (Graphically) | Draw the graphs of the two equations. <br> The solutions will be where the lines meet. <br> The solution can be written as a coordinate. |  $y=5-x \text { and } y=2 x-1$ <br> They meet at the point with coordinates $(2,3)$ so the answer is $x=2$ and $y=3$ |
| :---: | :---: | :---: |
| 7. Solving Linear and Quadratic Simultaneous Equations | Method 1: If both equations are in the same form (eg. Both $y=\ldots$ ): <br> 1. Set the equations equal to each other. <br> 2. Rearrange to make the equation equal to zero. <br> 3. Solve the quadratic equation. <br> 4. Substitute the values back in to one of the equations. <br> Method 2: If the equations are not in the same form: <br> 1. Rearrange the linear equation into the form $y=\ldots$ or $x=$... <br> 2. Substitute in to the quadratic equation. <br> 3. Rearrange to make the equation equal to zero. <br> 4. Solve the quadratic equation. <br> 5. Substitute the values back in to one of the equations. <br> You should get two pairs of solutions (two values for $x$, two values for $y$.) <br> Graphically, you should have two points of intersection. | Example 1 <br> Solve $\begin{aligned} & y=x^{2}-2 x-5 \text { and } y=x-1 \\ & \quad x^{2}-2 x-5=x-1 \\ & \quad x^{2}-3 x-4=0 \\ & \quad(x-4)(x+1)=0 \\ & x=4 \text { and } x=-1 \\ & y=4-1=3 \text { and } \\ & y=-1-1=-2 \end{aligned}$ <br> Answers: $(4,3)$ and $(-1,-2)$ <br> Example 2 <br> Solve $x^{2}+y^{2}=5$ and $x+y=3$ $\begin{gathered} x=3-y \\ (3-y)^{2}+y^{2}=5 \\ 9-6 y+y^{2}+y^{2}=5 \\ 2 y^{2}-6 y+4=0 \\ y^{2}-3 y+2=0 \\ (y-1)(y-2)=0 \\ y=1 \text { and } y=2 \\ x=3-1=2 \text { and } x=3-2=1 \end{gathered}$ <br> Answers: $(2,1)$ and $(1,2)$ |

