Maths Knowledge Organiser

8A1a.i: Properties of Number

| Factors | and | Multip | les |
|----------------|-----|--------|-----|
|----------------|-----|--------|-----|

| Factors and M | uitipies | |
|---------------|---------------------------|---------------------------|
| Factor | A number that | The factors of 18 are: |
| | divides exactly into | 1, 2, 3, 6, 9 , 18 |
| | another number | |
| | without a | The factor pairs of 18 |
| | remainder. | are: |
| | | 1 & 18, 2 & 9, 3 & 6 |
| | It is useful to write | |
| | factors in pairs | |
| Highest | The biggest number | The HCF of 6 and 9 is 3 |
| Common | that divides exactly | because it is the biggest |
| Factor | into two or more | number that divides |
| (HCF) | numbers. | into 6 and 9 exactly. |
| Multiple | The result of | The first five multiples |
| | multiplying a | of 7 are: |
| | number by an | |
| | integer. | 7, 14, 21, 28, 35 |
| | The times tables of | |
| | a number. | |
| Lowest | The smallest | The LCM of 3, 4 and 5 is |
| Common | number that is in the | 60 because it is the |
| Multiple | times tables of each | smallest number in the |
| (LCM) | of the numbers | 3, 4 and 5 times tables. |
| | given. | |

Powers

| Powers | | |
|-----------|----------------------------|---------------------------------|
| Square | The number you get | 1, 4, 9, 16, 25, 36, 49, |
| Number | when you multiply a | 64, 81, 100, 121, 144, |
| | number by itself. | 169, 196, 225 |
| | | $9^2 = 9 \times 9 = 81$ |
| Square | The number you | $\sqrt{36} = 6$ |
| Root | multiply by itself to | |
| | get another number. | because $6 \times 6 = 36$ |
| | | |
| | The reverse process of | |
| | squaring a number. | |
| Cube | The number you get | 1, 8, 27, 64, 125 |
| Number | when you multiply a | $2^3 = 2 \times 2 \times 2 = 8$ |
| | number by itself and | |
| | itself again. | |
| Cube Root | The number you | $\sqrt[3]{125} = 5$ |
| | multiply by itself and | |
| | itself again to get | because $5 \times 5 \times 5 =$ |
| | another number. | 125 |
| | | |
| | The reverse process of | |
| | cubing a number. | |
| Powers of | The powers of a | The powers of 3 are: |
| | number are that | $3^1 = 3$ |
| | number raised to | $3^2 = 9$ |
| | various powers. | $3^3 = 27$ |
| | - | $3^4 = 81$ etc. |

Primes

| number with exactly vo factors . | The first ten prime numbers are: |
|---|---|
| | numbers are: |
| 1 11 1 | |
| number that can only | |
| e divided by itself and | 2, 3, 5, 7, 11, 13, 17, |
| ne. | 19, 23, 29 |
| he number 1 is not | |
| rime, as it only has one | |
| ictor, not two. | |
| factor which is a prime | The prime factors of 18 |
| umber. | are: |
| | |
| | 2,3 |
| inding out which prime | 36 |
| umbers multiply | |
| gether to make the | (2) 18 |
| riginal number. | |
| | 2)9 |
| se a prime factor tree. | |
| | (3) (3) |
| lso known as 'prime | $36 = 2 \times 2 \times 3 \times 3$ |
| | |
| r h r | ne number 1 is not ime, as it only has one ctor, not two. factor which is a prime imber. Inding out which prime imbers multiply gether to make the iginal number. Se a prime factor tree. |

Fractions

| Tractions | | |
|-----------------|--|---|
| Fraction | A mathematical expression representing the division of one integer by another. Fractions are written as two numbers separated by a horizontal line. | ² / ₇ is a 'proper' fraction. ⁹ / ₄ is an 'improper' or 'top-heavy' fraction. |
| Numerator | The top number of a fraction. | In the fraction $\frac{3}{5}$, 3 is the numerator. |
| Denominator | The bottom number of a fraction. | In the fraction $\frac{3}{5}$, 5 is the denominator. |
| Unit Fraction | A fraction where the numerator is one and the denominator is a positive integer. | $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ etc. are examples of unit fractions. |
| Mixed Number | A number formed of both an integer part and a fraction part. | $3\frac{2}{5}$ is an example of a mixed number. |

Simplifying

| x tim | ies x | The answer is x^2 not | Squaring is multiplying |
|--------------|--------------|-------------------------|---------------------------|
| | | 2x. | by itself, not by 2. |
| $p \times p$ | $p \times p$ | The answer is p^3 not | If p=2, then |
| | | 3 <i>p</i> | p^3 =2x2x2=8, not 2x3=6 |
| p + p | p + p | The answer is 3p not | If p=2, then 2+2+2=6, |
| | | p^3 | $not 2^3 = 8$ |

Factorising

| Factorise | The reverse of | 6x - 15 = 3(2x - 15) |
|-----------|-----------------------------|-----------------------|
| | expanding. | 5), where 3 is the |
| | Factorising is writing | common factor. |
| | an expression as a | |
| | product of terms by | |
| | 'taking out' a | |
| | common factor. | |
| Quadratic | A quadratic | Examples of quadratic |
| | expression is of the | expressions: |
| | form | x^2 |
| | | $8x^2 - 3x + 7$ |
| | $ax^2 + bx + c$ | |
| | | Examples of non- |
| | where a , b and c are | quadratic |
| | numbers, $a \neq 0$ | expressions: |
| | | $2x^3 - 5x^2$ |
| | | 9x - 1 |

Rounding and Estimating

| Rounding | To make a number | 74 rounded to the |
|-------------|--|------------------------|
| | simpler but keep its | nearest ten is 70, |
| | value close to what it | because 74 is closer |
| | was. | to 70 than 80. |
| | If the digit to the right | 152,879 rounded to |
| | of the rounding digit is | the nearest |
| | less than 5, round down. | thousand is 153,000 |
| | If the digit to the right | |
| | of the rounding digit is | |
| | 5 or more, round up. | |
| Decimal | The position of a digit | In the number 0.372 |
| Place | to the right of a | the 7 is in the second |
| | decimal point. | decimal place. |
| | | 0.372 rounded to |
| | | two decimal places is |
| | | 0.37, because the 2 |
| | | tells us to round |
| | | down. |
| | | Careful with money |
| | | don't write £27.4, |
| | | instead write £27.40 |
| Significant | The significant figures | In the number |
| Figure | of a number are the | 0.00821, the first |
| | digits which carry | significant figure is |
| | meaning (ie. are | the 8. |
| | significant) to the size | |
| | of the number. | In the number 2.740 |
| | | the 0 is not a |
| | The first significant figure of a number | significant figure. |
| | cannot be zero. | 0.00821 rounded to |
| | | 2 significant figures |
| | In a number with a | is 0.0082. |
| | decimal, trailing zeros | |
| | are not significant. | 19357 rounded to 3 |
| | | significant figures is |
| | | 19400. We need to |
| | | include the two |
| | | zeros at the end to |
| | | keep the digits in the |
| | | same place value |
| | | columns. |
| Truncation | A method of | 3.14159265 can be |
| | approximating a | truncated to 3.1415 |
| | decimal number by | (note that if it had |
| | dropping all decimal | been rounded, it |
| | places past a certain | would become |
| | point without | 3.1416) |
| | rounding. | |

